

LECTURE 1: INTRODUCTION

> Space instruments are the links between :

- target
- missions
- data users
- spacecraft
- ...

> Two groups :

- ① Remote telescopes, imagers, radar, ...
- ② In situ magnetic field, gravitational field, ...

> A space experiment is :

- to realize an experiment outside Earth
- Observation of the Universe

> Types of scientific space missions :

- ① Earth observation
- ② Astrophysics
- ③ Planetary Science
- ④ Heliophysics

> We go to space because :

- ① Some things can't be done from Earth
- ② Unique environment
- ③ Pushing innovation
- ④ ...

> The atmosphere absorbs certain λ of the EM spectrum. This creates atmospheric windows

> The EM spectrum: shorter λ  longer λ

> Challenges :

- ① Go $\rightarrow$ Stay $\rightarrow$ Return
- ② Cost
- ③ Harsh environment
- ④ ...

> Observables :

- ① EM waves
- ② Static fields
- ③ Particles
- ④ Matter samples
- ⑤ Gravitational waves

> Instruments act as an information filter because they do not capture all of the information that exists (e.g. only a certain λ)

> The mission design process consists of :

- ① Mission analysis
- ② Feasibility
- ③ Preliminary definition
- ④ Design
- ⑤ Production
- ⑥ Operation
- ⑦ Disposal

O
A
B
C
D
E
F

> The TRL is a number associated with something which tells how far into development it is

↳ Range : 1 (basic principles) → 9 (flight proven)

> A **payload** is those elements dedicated to producing mission data and sending it back

LECTURE 2: ELM - SENSING THE BASICS

- > The cells in a scientific image is relative to the position on the detector, and the value corresponds to the number of received photons
- > The **field of view** is the angle of observation
- > The projected area on the ground is the **swath**
- > The **resolution** indicates the smallest feature that can be observed
- > The **sharpness** describes how well edges are perceived
- > The **contrast** is the difference between light/dark

↳ These five are indications of the **image quality**

> All objects can be observed by use of photons

↳ we do so from space mainly to get rid of the atmosphere

↳ we can get:

- Temperature
- Composition
- Motion
- ...

> Photon generation / absorption processes:

- ① Black body radiation
- ② Quantum transition
- ③ Acceleration of charged particles
- ④ Annihilation of (anti) matter

① ↳ BB radiation is most fundamental source of radiation

$$↳ L_{\lambda}(T) = \frac{2hc^2}{\lambda^5} \left[e^{hc/\lambda k_B T} - 1 \right]^{-1}$$

$$↳ \text{Wien: } \lambda_{\max} = \frac{b}{T}; \quad b \approx 0.028$$

> EM radiation is quantified

$$↳ E_{\nu} = h\nu = hc/\lambda$$

② ↳ Absorption causes an electron to move to an excited state with energy level:

$$↳ \Delta E = h\nu = E_1 - E_0$$

> Spontaneous emission is the opposite

> Stimulated emission is when incoming radiation causes a drop down

> A **light source** is a geometrical element out of which light escapes

↳ It can be from production, reflection, scattering

- > Light can be seen as : ① Ray
② Wave
③ Particle

Light as a Ray

- > Laws for geometrical optics : ① Reflection
② Refraction
③ Diffraction

① $\theta_i = \theta_r$

② $n_1 \sin \theta_i = n_2 \sin \theta_t$

③ $\sin \theta_{\text{diff}} \pm \sin \theta_i = \frac{m\lambda}{\lambda}$

> **Scattering** is a deflection not following reflection or refraction

$\tau \approx \frac{4\pi R^2}{\lambda}$

> The index of refraction is a function of the wavelength

$\hookrightarrow$ This causes **dispersion**



$\lambda_n = \frac{v}{f} = \frac{c}{nf} = \frac{\lambda}{n}$

> The **optical path length** is the length that light needs to travel through vacuum to create the same phase difference

$\delta(\lambda) = n(\lambda) \cdot l$

> **Fresnel reflection** is the reflection at the boundary of 2 media

$\text{Reflectivity} = \frac{I_r}{I_0} \cdot 100\%$

$\text{Transmittivity} = \frac{I_t}{I_0} \cdot 100\%$

$\hookrightarrow$ The process depends on the **polarization**, and we get r_s, r_p, t_s, t_p

> In total we have 3 processes : ① Reflection
② Transmission
③ Absorption

$\hookrightarrow$ The Beer-Lambert law : $T = \frac{I_t}{I_0} = e^{-\alpha}$

$\hookrightarrow$ Conservation of energy : $R + T + A = 1$

Light as a Wave

> Maxwell equations give a wave equation

> The Huygens principle states that every point on a wave acts as a point source

↳ Each point source creates a spherical wave of radius $r = v \cdot t$

↳ Rays are perpendicular to the wavefronts

↳ The Huygens principle explains **diffraction**, the bending of waves behind an obstacle

↳ The double slit experiment confirms it, making interference patterns

> In thin films, waves can also reflect

> Anti-reflective coatings are needed to avoid parasitic reflections

LECTURE 3 : IMAGERS

> **Earth observation** is the gathering of information about the Earth

↳ Imagers can be used

> The general concept of imagers is to collect photons, focalize them to a detector and converting to electrons, ^{→ detector} and numerize it for data storage and transfer ^{→ camera}

→ telescope assembly

> To create optical space instruments, we need :

- ① Radiometric budget
- ② Optical system
- ③ Detector system

> The **resolution** is the ability of an optical system to return the information contained into an optical scene

↳ Types :

- ① Spatial / Resolving Power
- ② Radiometric
- ③ Spectral
- ④ Polarimetric

distance
photons
wavelength
stokes vector

Paraxial Optics

> A **lens** has the properties :

- ① f
- ② R_1
- ③ R_2
- ④ d
- ⑤ n

↳ Lensmaker's equation : $f^{-1} = (n-1) \left(R_1^{-1} - R_2^{-1} + \frac{(n-1)d}{n R_1 R_2} \right)$

> Paraxial optics is used for image formation and size magnification, not quality

> Rays remain close to the optical axis

↳ $\sin \theta \approx \theta$; $\tan \theta \approx \theta$

> Can determine :

- ① Location of object / image planes
- ② Clear aperture
- ③ Optical power
- ④ Magnification
- ⑤ Separation
- ⑥ Radiometric calculation

↳ Analysis of optical aberration is required for image quality

> The paraxial approximation basics are :

① Geometrical optics domain

↳ λ is small compared to objects $\Rightarrow$ light is a ray

② Optical path depth

$$\hookrightarrow \delta = \int_A^B n(s) ds$$

③ Fermat principle

$\hookrightarrow$ Light chooses the path which minimizes the time to go from point A to point B

④ Stigmatism

$\hookrightarrow$ The image of a point is a point

> For image formation with a lens, a graphical paraxial ray trace gives 3 rays:

- ① Parallel to optical axis
- ② Passing through the center
- ③ Passing through the object focus

> Magnification:

① Transverse

$$\hookrightarrow m = g_y = \frac{\overline{A'B'}}{\overline{AB}} = \frac{y'}{y} = -\frac{d_i}{d_o}$$

② Axial

$$\hookrightarrow m = g_z = \frac{\Delta z'}{\Delta z} = g_y^2$$

> A **virtual image** is an image through which light does not go

> A **real image** is the collection of focus points made by converging rays, while a VI is the collection of focus points made by extensions of diverging rays

> Thin lens equation: $d_i^{-1} + d_o^{-1} = f^{-1}$

$$\hookrightarrow m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

> For a source located at infinity, all rays can be considered parallel

$\hookrightarrow$ For an extended source, the information is angular

$\hookrightarrow$ Optical systems convert angular into a spatial information

$$\hookrightarrow x = f \tan \theta$$

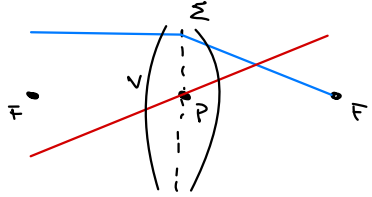
> The **pixel sampling distance** is the size of a projected pixel

- > The **spatial resolution** is the smallest ground feature that can be resolved
- > The **swath** is the total ground width captured by the FOV

$$\hookrightarrow \frac{GSP}{h} = \frac{PS}{f} = \tan \alpha$$

- > As a spacecraft orbits, it covers one direction of motion. To scan the ground, a 1D sensor can be used
- > An optical system can be replaced by its cardinal points and planes

- ① Focus F
- ② Principal point P
- ③ Principal plane Σ
- ④ Nodal points P'
- ⑤ Thin lens limit V



- > The optical power

$$\hookrightarrow \varphi = (n-1) \left(C_1 - C_2 + \frac{n-1}{n} t C_1 C_2 \right)$$

- > Two rays describe a system: ① **Chief** Edge → center
② **Marginal** Center → Edge

- > The **entrance pupil** is the image of a stop upstream
- > The **exit pupil** is the image of a stop downstream
- > The **aperture stop** is the physical aperture that limits the bundle of rays
- > A **field stop** limits the angular size of an object
- > The F-number is the ratio between the focal length and the entrance pupil

$\hookrightarrow$ Impacts the diffraction effect on the focal plane

- > The **spectral domain** is determined by: ① Source
② Transmission
③ Detector
④ Polarization

Aberration

- > Aberrations are deviations from the paraxial ray trace

$\hookrightarrow$ Depends on: ① Optics shape
② Fields
③ wavelength
④ Aperture size

- > Chromatic effects happen because of varying n with λ

- > Third order aberration happens due to the small angle approximation
- > Spherical ^{on axis} aberration is due to a spherical shaped optical surface
- > Astigmatism is a form of off axis aberration
- > Due to wave properties and aberration, the image of a point is not a point
- > Airy function: $r = 1.22 \frac{f\lambda}{D} = 1.22 F\# \lambda$
- > The Rayleigh criterion states that two points are considered resolved if the maximum of one is not closer than the first minimum of the other
- > The point spread function is a 2D distribution of light intensity
- ↳ $S_i(e) = e * h_i$
- > The modulation transfer function indicates the ability of an optical system to transfer the frequency information
- ↳ The optical transfer function is the Laplace transform of the PSF
- ↳ $OTF = MTF e^{i \text{PSF}}$

LECTURE 4: OPTICAL COMPONENTS

> In general, a lens works by the Snell-Descartes law

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

> For an incident collimated beam, we can draw out a selection of rays, and find they come together at some point, the focal point

↳ Simplified: use lensmaker formula

↳ Based on basic ray tracing

> For more than 1 λ , we have aberration happening

↳ This gives multiple focal lengths (1 per λ)

↳ f increases with λ

↳ To solve, we can add a compensating lens

↳ For lens combination:

$$\frac{1}{f_{\text{eff}}} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

↳ We thus use 2 different materials to compensate dispersion

> Note that no lens is 100% achromatic

↳ Because of this, in space often mirrors are used

↳ Different shapes are used:

- ① Flat
- ② Spherical
- ③ Parabolic
- ④ ...

> For a spherical mirror: $f = -0.5 R_c$

↳ For small f /dbeam, the outer rays do not have the same f

↳ This is spherical aberration, and why we use other surfaces

↳ Parabolic mirrors have a single focal point

> Other reasons for mirrors:

- ① Segmented / Folded is space proof
- ② Coatings can be adapted

Materials

> A material is not transmissive in the entire EM spectrum

↳ $n = \eta + i\kappa$, with κ the absorption coefficient

↳ For the electric field:

$$E = E_0 e^{ik\eta z - i\omega t} = E_0 \underbrace{e^{-\kappa \kappa z}}_{\text{Decrease due to absorption}} e^{ik\eta z - i\omega t}; \kappa = \frac{2\pi}{\lambda}$$

↳ Intensity:

$$I = |E|^2 = |E_0|^2 e^{-2\kappa \kappa z} = I_0 e^{-2\kappa \kappa z}$$

> Different materials can be chosen for transmissive optics, depending on bandwidth, availability, budget, and desired application

> For reflective optics, most of the shape is given by the substrate attached to the mount

↳ It is submitted to σ and ΔT which put requirements on it

> Coatings inherit the deviations of the substrate

> Metallic coatings are for broadband reflection

> Dielectric coatings are for specific bandwidths

> Reflection happens in transmissive optics (Fresnel)

↳ To find the transmitted field, we look at reflection at the interfaces, and absorption in the medium

> Parasitic reflection is when part of the incident signal is reflected

↳ This causes less signal on the detector, and the possibility of a fake signal **ghost**

↳ To reduce the effect, anti-reflective coatings can be used

↳ They work by adding a layer which creates a second reflection which cancels the first **destructive interference**

$$\Delta \varphi = \pi$$

↳ Thumb rule:

$$n_{\text{coating}} = \sqrt{n_{\text{air}} n_{\text{sub}}}; \quad h \sim \frac{\lambda}{4}$$

Polarization

> Light consists of:
① Electric field
② Magnetic field

↳ The two fields are perpendicular to each other and the propagation direction

> Polarizers select only one type of polarization and change the intensity of light

> Birefringent plates change the polarization state

> Polarizers are characterized by: ① Transmission axis
② Absorption axis ($\perp$)

↳ Only the vibration parallel to the transmission axis is transmitted

$$\hookrightarrow \vec{E}_{out} = \vec{E}_{in} \cos \theta ; I_{out} = I_{in} \cos^2 \theta$$

> Polarizers by absorption have long molecules inside which absorb the parallel vibration

↳ This results in linearly polarized output in direction of transmission axis

> A birefringent component has anisotropy in the crystal, and presence of 1 particular direction inside the component optical axis

↳ Light experiences 2 non-parallel resistances: ① Strong bonds
② Weak bonds

↳ We get 2 speeds in the material

$$\hookrightarrow \Delta n = |n_o - n_e| ; n = \frac{c}{v}$$

↳ The optical axis is parallel to the interface

↳ After the plate, there is a shift between the states

$$\hookrightarrow \Delta x = d(n_o - n_e)$$

↳ This creates a phase shift

$$\hookrightarrow \Delta \phi = \frac{2\pi}{\lambda_v} \Delta x$$

> Other polarization effects: ① Reflection
② Dichroism
③ ...

Diffraction Gratings

> Diffraction gratings are repetitive arrays of diffractive elements (apertures or obstacles) that result in periodic alterations in phase, amplitude, or both of an emergent wave

> Looking at narrow slits with normal incidence using the Huygens principle and interferometry, we get that each slit acts as a point source, and each sub-source emits several rays

↳ Each set of parallel rays recombines to make an equivalent wavefront

↳ There is a phase difference:

$$\Delta x = d \sin \theta = m \lambda$$

↳ For normal incidence, 1 beam is split into several beams

↳ For polychromatic, 1 beam is split along the period

↳ For non-normal, the working principle is the same

> Amplitude grating causes periodicity realized by a succession of opaque and transmissive area

> Phase grating causes periodicity realized by a variation of phase, and with that of optical path

> Diffraction grating can happen with transmission and reflection

> Used for spectroscopy to split the light by λ

Optical Filters

> Types:

- ① Short pass
- ② Long pass
- ③ Bandpass
- ④ Notch
- ⑤ Neutral densities

① ↳ High transmission at low λ , low transmission at high λ

② ↳ Low transmission at low λ , high transmission at high λ

③ ↳ Only transmits a certain bandwidth

④ ↳ Only blocks a specific bandwidth

⑤ ↳ Constant attenuation for large bandwidth

↳ Avoid detector saturation

LECTURE 5: RADIOMETRY

Transmittance and throughput need to be considered before building an instrument to evaluate the number of photons reaching the detector

↳ Too few photons $\rightarrow$ low SNR (or no signal at all)

↳ Too many photons $\rightarrow$ Saturation and possibly destruction of the detector

> The system spectral transmittance is:

$$\text{↳ } T(\lambda) = \frac{P_{\text{out}}(\lambda)}{P_{\text{in}}(\lambda)} \quad [-]$$

↳ P_{out} is the spectral radiant power at the focal plane

↳ P_{in} is the spectral radiant power falling in the entrance aperture

↳ Determined by: $\left. \begin{array}{l} \text{① Spectral transmittance} \\ \text{② Spectral reflectance} \\ \text{③ Spectral absorbance} \end{array} \right\} \text{ of each optical element}$

$$\text{↳ } R(\lambda) = \prod R_i(\lambda) ; T(\lambda) = \prod T_i(\lambda)$$

> There is a source of EM waves/photons $\rightarrow$ losses $\rightarrow$ Gathering
 $\rightarrow$ Spectral filter $\rightarrow$ Detector

> In addition to image quality, the amount of light reaching a detector is important

> A beam can be defined by two elements of area:

↳ This is the locus of possible rays that pass through the two areas separated by a distance d

↳ Each ray is defined by a vector and transports energy

> A **point source** is a small source of light that radiates equally in all directions

$$\text{↳ } h_x h_y \ll R^2$$

> An **extended source** is any source having measurable dimension

> Angles: ① Plane • $\varphi = \frac{s}{R}$ [rad]

② Solid • $\Omega = \frac{A}{R^2}$ [sr]

> The **F-number** • $F\# = \frac{f}{D} = (2 \sin \Theta_{1/2})^{-1}$

> The **numerical aperture** is a dimensionless number characterizing the range of angles accepted by the system

$$\hookrightarrow NA = n \sin \theta_{1/2}$$

$$\hookrightarrow \Omega = \frac{\pi}{4(\frac{r}{R})^2} = \frac{\pi (NA)^2}{n^2}$$

Radiometry of Point Sources

> The **luminosity** or **radiative flux/power** Φ_e is the amount of energy per unit of time leaving the source

> The **point source** or **radiant intensity** I_e is the power per unit solid angle

$$\hookrightarrow I_e = \frac{d\Phi_e}{d\Omega}$$

> The **irradiance** E_e is the illumination by a point of a surface placed at a distance R

$$\hookrightarrow E_e = \frac{\Phi_e}{A_i}$$

> Considering an isotropic emission of a point source:

$$\hookrightarrow I_e = \frac{\Phi_e}{\Omega}$$

$\hookrightarrow$ At a distance R_i :

$$\hookrightarrow E_e = \frac{I_e}{R_i^2} \quad \text{inverse square law}$$

$\hookrightarrow$ Trajectory is spherical, but most surfaces are flat $\Rightarrow$ correction needed

$\hookrightarrow$ If $A \perp R$, A' as $\odot$ with radius, then $R' > R$ and $A' > A$

$$\hookrightarrow E_e' = \frac{\Phi_e}{A'} = E_e \cos^3 \theta$$

Radiometry of Extended Sources

> For extended sources, there are some degrees of variation in the amount and direction of emission and with position

> The **radiance** or **brightness** $L_e = \frac{\Phi_e}{A_s \Omega}$

> An extended source can be seen as an area with a large collection of point sources distributed uniformly

$\hookrightarrow$ If each ΔA contains a point source with an I_e constant in all directions, the brightness of the sources in a normal direction is:

$$\hookrightarrow L_e(\theta) = \frac{\Phi_e}{\Delta A \Omega} \rightarrow \text{At an angle: } L_e(\theta) = \frac{L_e(0)}{\cos \theta}$$

> A **Lambertian source** can be used as an approximation

$$\hookrightarrow I_e = \frac{\Phi_e}{\Omega} \cos \theta; L_e(\theta) = L_e(0)$$

In Optical System - Point Source

> Behind the optical system exists another point source, the image

> From conservation of energy:

$$\hookrightarrow \phi_e = \frac{I_e A_1}{t_0^2} = \frac{I_e' A_1}{t_1^2} ; I_e' = I_e \frac{t_1^2}{t_0^2} = M^2 I_e$$

$\hookrightarrow$ transverse magnification of the system

> Entrance and exit pupils are important for calculating radiometry

In Optical System - Extended Source

> In the image space the observer sees an image if light is redirected

> For passive components:

$$\hookrightarrow \phi_e' = T \phi_e$$

$\hookrightarrow$ Transmittance of the system

> We can obtain the Etendue law:

$$\hookrightarrow A \Omega = A' \Omega'$$

$$\hookrightarrow L_e' = T L_e$$

$\hookrightarrow$ Etendue ($A \Omega$) is conserved (aka area-solid angle conservation)

Pupils and Apertures

> Finite nature of lenses and mirrors induces that they collect only a fraction of the energy emitted by a point source $\rightarrow$ clear aperture

> Any element that limits the amount of light reaching the image plane is an aperture stop

$\hookrightarrow$ Limits the light gathering capabilities

> A field stop determines the FOV of the instruments

> Pupils determine whether or not a given ray will go through the entire optical system and reach the focal plane

> The image of the stop is seen from an axial point

$\hookrightarrow$ In object space: entrance pupil

$\hookrightarrow$ In image space: exit pupil

Photon Noise

> Photon noise is the result of the discrete nature of the radiation

$\hookrightarrow$ Poisson distribution describes the probability:

$$\hookrightarrow p(i) = \frac{s^i}{i!} e^{-s}$$

From that:

$$\hookrightarrow \sigma_s = \sqrt{s}$$

$$\hookrightarrow \text{SNR} = \frac{s}{\sqrt{s}} = \sqrt{s}$$

LECTURE 6 · SPECTROSCOPY

- > Spectroscopic information is the decomposition of light on a spectrum
- > Spectroscopy is the study of physical phenomena over a frequency spectrum based on a wave process
- > Each material has its own unique set of spectral lines
 - ↳ Emission / absorption are the basis of spectroscopy
- > Schrödinger's Equation:

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle \quad \hbar = \frac{h}{2\pi}$$

↳ If H is independent of time → stationary solution

↳ Separation of time dependent solutions and space:

$$\psi(\vec{r}, t) = \psi(\vec{r}) e^{iEt/\hbar}$$

↳ $H\psi = E\psi$ time-independent Schrödinger Equation

↳ Solutions are a set of ψ_n associated with state energy set E_n

> Lecture 2 gave definition of absorption and (stimulated) emission

> A spectral line extend over a range of frequencies

↳ g_i correspond to degeneracy of the energy levels

↳ Degeneracy: one single value of E , while multiple λ

↳ The center may be shifted from its nominal central λ (Doppler shift)

↳ Reasons of broadening: ① Thermal Doppler

② Natural

③ Pressure / Collisional

Molecular Spectra

> The complexity increases with many-atom systems:

① Broken symmetry: ① Atom: spherical symmetry

② Diatomic: in-line symmetry

③ Other: More complex

② Quantum transitions involve rotations and vibrations

③ Orbitals for electronic transitions are built differently

↳ There are group vibrations

> We have:

↳ Energy $\Delta E = h\nu = \frac{hc}{\lambda}$

↳ Wave number $\sigma = \frac{1}{\lambda} = \frac{\Delta E}{hc}$

> The electronics, vibrational, and rotational energies are independent

↳ $E = E_{el} + E_{vib} + E_{rot}$

↳ $\Psi_{tot} = \Psi_{el} \cdot \Psi_{vib} \cdot \Psi_{rot}$

> A change of E_{tot} is then:

↳ $h\nu = hc\sigma = \Delta E = E' - E'' = \sum E'_i - E''_i$

> For an electronic transition, there is a general structure

> For a vibrational transition, there is a coarse structure

> For a rotational transition, there is a fine structure

Spectroscopic Instruments

> A **spectroscopic instrument** is a scientific instrument used to split the light into an array of separated colors → **spectrum**

↳ A spectrum shows the intensity of light in function of λ and f

↳ Light deflection and separation is produced by a Prism or diffraction grating

> A **spectrometer** consists of:

- ① Dispersion element
- ② Pupils (from stops)
- ③ Optical interfaces

Additional Subtilities

> A slit can be added at the entrance and exit

↳ $\tan \theta_{col} = \frac{S_i/2}{f_{col}} = \frac{S_e/2}{f_{col}}$

↳ The intensity profile shows the transmission through the slit for each λ

> A prism causes diffraction as seen before

↳ $n(\lambda) \Rightarrow \Theta(\lambda)$

> Grating also results in diffraction

↳ $\sin \Theta_{diff} \pm \sin \Theta_i = \frac{m\lambda}{\Lambda}$

- 4 Different gratings exist:
- ① Sawtooth
 - ② Sinusoidal
 - ③ Laminar
 - ④ Phase

4 The diffraction efficiency is given by:

$$4 \eta^m(\lambda) = \frac{I^m(\lambda)}{I_0(\lambda)}$$

> The diffraction of a laser spot by a circular aperture is on Airy disk

4 The angle at which the first minimum occurs:

$$4 \sin \theta \approx \theta \approx 1.22 \frac{\lambda}{d}$$

4 The resolution is limited due to the diffraction of light

4 With an aperture w : of finite size, we are diffraction limited

$$4 \Delta_{\text{Airy}} = 2.44 \frac{f \lambda}{w}$$

$$4 \text{ linear dispersion} = \frac{\Delta \lambda}{\Delta x}$$

> The resolving power,

$$4 R = \frac{\lambda}{\Delta \lambda}$$

4 The Rayleigh criterion should be verified

LECTURE 7: DETECTORS

- > Objects radiate, which we want to detect, and thus we need **detectors**, to create a visual representation of the observed scene
- > A detector uses the principle of converting an input signal into a representative electronic output signal

4 Different principles:

① Photo-emission	0.1 - 5 μm
② Internal photo-electric effect	0.5 - 10 μm
③ Thermal	0.5 - 1000 μm

> Single element detectors generate an output signal proportional to the total power collected

↳ categories

> Image detectors have an active area physically divided

Detector Types

- ① Thermal
- ② Photon based
- ③ Semiconductor based focus

> The photo-electric effect is a phenomenon which occurs when high energetic light hits a material and electrons are ejected

- 4 ① e^- are bound to valence band
- ② Added energy
- ③ e^- get excited and go to conduction band

4 There is an energy difference E_{gap} depending on material

4 The photon energy is more than E_{gap}

$$4 E_{\text{ph}} = \frac{hc}{\lambda} > E_{\text{gap}}$$

> The detectivity is an indication of how well a detector can detect weak signals in presence of noise

> The lattice constant is a physical dimension defining the size and shape of the smallest repeating unit

4 Typically the band gap depends on this, but not for MCT

> A **photoconductor** is the cheapest approach for photon detection

4 Semiconductor is illuminated, and generates a current

4 Consist of a thin layer of semiconductor material

4 Conductance varies with photon flux

↳ The semiconductor absorbs light causing the conductivity to rise

↳ They are typically low performance due to the high noise levels

$$V_S = -\Delta i \cdot R$$

↳ Read-out is done by use of processing and an ADC

> **Photodiodes** are more accurate

↳ They have:

- ① + Higher speed
- ② + Lower noise
- ③ + Better sensitivity
- ④ - Difficult fabrication
- ⑤ - Expensive

↳ Consist of 2 layers on top of each other, each doped with additional materials

n: extra e^-
p: extra holes

↳ An electric field is generated between the n and p layers pulling e^- from the junction

↳ A PIN photodiode adds an **intrinsic layer** between the other 2 to increase efficiency

↳ An APD has an additional (n total) layer, causing it to generate more than 1 e^-

↳ Read-out is similar as for photoconductors

> **CCD detectors** consist of an array of linked capacitors

↳ External circuit is required

↳ Each pixel has an absorbing semiconductor

↳ All accumulated e^- are converted to an output voltage

↳ Read-out consists of control logic, ...

↳ Binning combines charge of adjacent pixels during readout

> **CMOS detectors** are similar, but voltage conversion happens in each pixel

↳ They can access each pixel in random order

> **Hybrid detectors** integrate CCD and CMOS on the same chip

Signal to Noise

$$> S = I_s \cdot t \cdot QE$$

> Noise :

- ① dark

$$n = \sqrt{I_{\text{dark}} \cdot t} / q$$

- ② shot

$$n = \sqrt{S} = \sqrt{n_{\text{total}} \cdot A \cdot \frac{A\nu}{h\nu} \cdot F_v \cdot t \cdot QE}$$

- ③ Thermal background

$$n = \sqrt{I_{\text{back}} \cdot t} / q$$

- ④ Electronics

- ⑤ Conversion

$$n = \sqrt{kTC} / q$$

$$N = \sqrt{\sum N_i^2}$$

$$SNR = \frac{S}{N}$$

LECTURE 8: POLARIZATION

> The study of polarization relates to the evolution through time of the vector describing the EM field at one point in space

> We start with Maxwell's equations in vacuum:

$$\nabla \cdot \vec{E} = 0$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \cdot \vec{B} = 0$$

$$\nabla \times \vec{B} = \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

↳ We can find for a light beam propagating in z-direction, in free space, for the monochromatic case, the electric field is:

$$\vec{E} = E_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \quad \text{sinusoidal plane wave}$$

$$\vec{E} = E_x \cos(kz - \omega t) \hat{x}_0 + E_y \cos(kz - \omega t + \Delta\phi) \hat{y}_0 \quad \text{real part}$$

> Optical components are sensitive to polarization, information on the atmosphere is found using it, and more

> The **polarization state** of the field is contained in the temporal variations of the amplitude vector

> There are 3 states: ① Elliptical

② Linear

③ Circular

general

$$E_x = 0, E_y = 0, \text{ or } \Delta\phi = m\pi$$

$$E_x = E_y \text{ and } \Delta\phi = (2m+1)\frac{\pi}{2}$$

$$\frac{\omega}{k} > 0: \text{ccw}, < 0: \text{cw}$$

↳ Shapes are the map of the field on a plane over time

> There is a variation of scattered and absorbed light because biological material does not interact the same with left or right circular

> Light coming from the Sun/lamp is emitted by several independent emitters, thus there is no relation between E_x , E_y , and $\Delta\phi$, meaning the light can have every polarization state

↳ Every 10 ns, E_x , E_y , $\Delta\phi$ for one emitter change

↳ **Unpolarized light** has every polarization state without preference, and they change quickly

> The degree of polarization (0-1) indicates how much light is polarized

> Also a degree of linear polarization

> Polarization is quantified using the preferred direction α

> Polarization can be changed using a linear polarizer which blocks one direction of the vibration

> Common detectors measure the intensity, not the electric field

$$\propto I = \epsilon_0 c \langle E^2 \rangle_T$$

$$\propto I = A |E|^2$$

Phase Retarders

> light has different propagation speeds depending on incident polarization

↳ There are 2 axes: ① Fast (small n)
② Slow (large n)

↳ **phase retarders** give $\vec{E}$ along the slow axis an extra $\Delta\phi$, changing the phase

↳ A retarder with a slow horizontal axis and a $\Delta\phi$ produces the same state as one with a fast vertical axis and $\Delta\phi$

↳ When $\Delta\phi = \pi$, the retarder is a **half-wave plate**

↳ linear: rotates with 2θ

↳ circular: ccw $\leftrightarrow$ cw

↳ when $\Delta\phi = \frac{\pi}{2}$, the retarder is a **quarter-wave plate**

↳ linear: to circular if $\theta = \pm 45^\circ$, else to elliptical

↳ circular: to linear

Measuring

> **Polarimetry** is the determination of the polarization state of a beam

↳ Different methods: ① Sequential measurements
② Division on detector
③ Spectral/Polarization modulation
④ ...

① ↳ Simplest method: using a linear polarizer on a rotating mount
↳ The detector has sequential acquisition at different orientations
↳ Can not solve $\Delta\phi$, and can't differentiate circular from natural
↳ A more advanced form is a fixed linear + rotating $\lambda/4$
↳ This can identify every state, and $E_x, E_y, \Delta\phi$ can be found with Fourier

② ↳ Camera with integrated pixelated polarizer

- ↳ Each pixel has different angles, thus a snapshot can be used to determine polarization state
- ↳ Some resolution is lost
- ↳ Can not differentiate circular vs unpolarized

Components

- > Diffraction gratings in reflection are polarization sensitive
- ↳ Measurement and detection are necessary for measurements

Atmosphere

- > The Sun yields unpolarized light
- ↳ The oscillation of electric dipoles is parallel to the vibration direction
- ↳ Re-radiation happens in a plane perpendicular to the vibration, and a reduced intensity in observation direction
- ↳ There is no emission in vibration direction
- ↳ Depending on observer position, some parts acquire a preferential orientation for the electric field → partial polarization

LECTURE 9: INTERFEROMETRY

> we know waves have a wavelength and a frequency **related**

> Waves are subject to superposition: ① Constructive interference
② Destructive interference

↳ For interference: ① ≥ 2 waves
② Same frequency
③ Coherent **definite phase relation**

$$> E = E_1 + E_2$$

$$↳ I = I_1 + I_2 + \underbrace{2\sqrt{I_1 I_2} \cos \Delta\phi}_{\text{interference term}}$$

↳ If $I_1 = I_2 = I_0$:

$$↳ I = 2I_0(1 + \cos \Delta\phi) = 4I_0 \cos^2\left(\frac{\Delta\phi}{2}\right)$$

> Detection of light is an integrating process **in space and time**

↳ Time: A detector needs a certain amount of time to collect enough photons

↳ Space: A detector has a finite size

> The **coherence of light** is the degree to which waves in a beam maintain a consistent phase relationship

> **Temporal coherence**: How well ϕ is predictable over time

↳ High: fixed fluctuation in spacing of wavefronts

↳ Low: Random fluctuation in spacing of wavefronts

> **Spatial coherence**: How well ϕ is predictable in space

↳ High: fixed fluctuation in the shape of wavefronts

↳ Low: random fluctuation in the shape of wavefronts

> In an interferometer, the same source is split and recombined to interfere

↳ ① Wavefront division interferometers **e.g. double slit**
② Amplitude division interferometers

① ↳ Young's Double Slit

↳ Path difference: $d \sin \theta = n\lambda$; $\theta \approx \frac{x}{L}$ **$n \in \mathbb{N}$ for bright
 $n \in \mathbb{N} + \frac{1}{2}$ for dark**

② ↳ Michelson Interferometer

↳ use of beam splitter and mirrors

Detection of Gravitational Waves

> Gravitational Waves are ripples in space-time

↳ Strength is characterized by strain amplitude

$$h_0 = \frac{\Delta L}{L}$$

↳ Even for large L , ΔL is very small

↳ we use Michelson interferometer to measure with suspended test masses

$$E_{out} = -i E_{in} e^{i 2 k L} \sin(2 k \Delta L)$$

$$P_{out} = P_{in} \sin^2(2 k \Delta L)$$

↳ we measure $\Delta \phi$ using the induced displacement

$$\Delta \phi = \frac{4\pi}{\lambda} \Delta L$$

↳ As we measure ΔL and h_0 is fixed, we increase L to get a larger ΔL (easier to measure)

↳ Done through adding additional mirrors

$$\Delta \phi = \frac{4\pi}{\lambda} \Delta L = \frac{4\pi}{\lambda} h_0 L_{eff} ; L_{eff} = \frac{2F}{\pi} L$$

↳ The mirrors create a Fabry-Pérot cavity, allowing the longer length

↳ Resonance occurs in the cavity when the light constructively interferes

$$FSR = \frac{\Delta \lambda}{\delta \lambda}$$

$$F = \frac{\pi \sqrt{r_1 r_2}}{1 - r_1 r_2}$$

↳ we have three parts of the beam:

- ① Reflected
- ② Transmitted
- ③ Circulating

$$E_{refl} = -r_i E_{in} + t_i r_e e^{i 2 k L} E_{circ}$$

$$E_{trans} = t_e E_{circ}$$

$$E_{circ} = t_i E_{in} + r_i t_e e^{i 2 k L} E_{circ}$$

↳ Typically $r_i r_e$ is chosen to be around 1, making it such that there is resonance when $L = \lambda/2 \cdot n$

> GW interferometers suffer from noise

Interferometry in Space

① LISA is a GW interferometer in space

- ↳ Ground-based are sensitive in a small bandwidth only

> The induced $\Delta\phi$ is related to the frequency

$$u \quad \varphi_{G\omega} = 2\pi f_{G\omega} t = 2\pi f_{G\omega} \frac{L}{c}$$

↳ In space, we can have much larger L , and there is less noise

= Two types of scattering: ① Specular smooth
② Diffuse rough

↳ Stray light is caused by scattering, ghost beams, transmitted beams

4 Coherent scatter occurs when stray and main have same Δp

4 Incoherent scatter, when not

4 Required Surface Smoothness:

$$u \delta L = \sqrt{\frac{P_{ST}}{P_{MB}}} \delta x$$

② Nulling interferometry for detection of exoplanets

4 Requirements :

- ① High spatial resolution
- ② High contrast performance
- ③ High sensitivity

4 Detection done with nulling interferometry

4 2 telescopes collect light of star and planet, with interferometer designed to destructively interfere the light of the star, and constructively the planet light

- High spatial resolution requires large baseline

White light Interferometry

=> For GW detection we use high coherence interferometry

4 A high coherence source has high temporal and spatial coherence

6 A low coherence source only has high spatial coherence

> White light interferometry is used for surface height measurements

↳ Normally a laser is used as input because of its narrow optical spectrum

4 For WLI, a broadband source is used

↳ It is split into the arms, and a reference mirror can be moved as a function of the optical path difference

$$\Delta \phi = \frac{2\pi}{\lambda} \Delta z = \frac{2\pi}{\lambda} (z_R - z_S)$$

↳ The interfering beam is measured

$$I(z_{m_1}, z_{m_2}) = S_0 \left(R_{M_1} + R_{M_2} + 2\sqrt{R_{M_1}R_{M_2}} e^{-\frac{(z_{m_1} - z_{m_2})^2 \Delta k^2}{2}} \cos(2k_0(z_{m_1} - z_{m_2})) \right)$$

↳ For monochromatic, the exponential is 1

↳ For broadband, the interference of all colors is combined

↳ An **interferogram** is a localized interference pattern around zero OPD for a broadband light source

$$\Delta z = \frac{2 \ln(2)}{\pi} \frac{\lambda_0^2}{\Delta \lambda}$$

↳ This gives the OPD range over which interference occurs

- > we can use this to see the reflectivity of different surfaces
- > to examine the different layers in the eye

LECTURE 10: OPTICAL COATINGS

- > When light interacts with matter :
- ① Absorption
 - ② Reflection / scattering
 - ③ Transmission

> Waves :

$$\lambda = \frac{c}{f} ; \lambda' = \frac{c}{nf}$$

$$OT = nd$$

↳ Refraction happens because velocity changes

$$n = \frac{c}{v} = \sqrt{\frac{\epsilon_r \mu_r}{\epsilon_0 \mu_0}} = \sqrt{\epsilon_r \mu_r}$$

↳ Electric permittivity ↳ Magnetic permittivity

> Energy must be conserved

$$E = hf = \frac{h\nu}{\lambda} \Rightarrow f \text{ needs to change}$$

> There is total internal reflection for :

$$\theta_c = \arcsin\left(\frac{n_1}{n_2}\right)$$

Electromagnetic Wave Boundary Conditions

> To determine field magnitudes we need the BCs at the interface

↳ For charge accumulation $\vec{E}_1 \neq \vec{E}_2$

$$\epsilon_1 E_{1\perp} = \epsilon_2 E_{2\perp}$$

$$E_{1\parallel} = E_{2\parallel}$$

↳ For normal incidence :

$$\frac{E_R}{E_T} = \frac{n_1 - n_2}{n_1 + n_2}$$

↳ If $n_1 < n_2$, there is a phase flip

↳ For a thin film, we generally have a phase flip ($n_{\text{film}} > n_{\text{air}}$) at the top surface but not at the bottom,

↳ For very thin films, the two reflections will destructively interfere

$$E_{\text{tot}} = E_{\text{tr}} \left(-1 + T^2 \cos \frac{2\pi d}{\lambda} \right)$$

> At the polarization angle, p-polarized light will not be reflected if :

$$\theta_B = \arctan \frac{n_2}{n_1}$$

↳ At this angle there is pure s-polarized reflection

Thin Film Coatings

> Can create

- ① anti / high reflection
- ② wavelength selective

↳ Materials define refractive indices and interference (reflection)

> Coatings are used to enhance:

- ① Reflection
- ② Transmission
- ③ Absorption
- ④ Polarization

↳ Constructed by:

- ① Thin layers of dielectrics
- ② Thick layer of metal
- ③ Combinations

① ↳ Utilize interference

② ↳ **First surface mirrors** cause pure reflection

↳ **Second surface mirrors** have a ghost reflection as the light is first passed through a substrate

↳ A second surface can protect the coating

Single and Multi-layer Optical Coatings

> Anti-reflective coatings use destructive interference in a film

$$\Delta\phi = 2tn_c$$

> Intensity of a reflected beam

$$I = \left(\frac{1-p}{1+p} \right)^2 \cdot I_0 ; p = \frac{n_1}{n_2}$$

↳ For equal intensity, $\frac{n_1}{n_2} = \frac{n_2}{n_3}$

$$\text{Simplest: } n_{\text{film}} = \sqrt{n_{\text{substrate}}}$$

> OPD is a function of the angle (higher for higher), causing a phase difference per angle

↳ Complete cancellation can be achieved with ≥ 2 layers

↳ Two-layer AR coatings are the simplest form of **V-coatings**

↳ On JWS, $\lambda > 400 \text{ nm}$ has nearly no reflection due to ZARC

> A quarter wave stack is a dielectric multilayer system for high reflective coatings

↳ Has alternating layers of high and low index layers with $OPD = \frac{1}{2}\lambda$

↳ Highly reflecting for λ_{des}

↳ Based on constructive interference

$$R = \left[\left(1 - \left(\frac{n_H}{n_L} \right)^{2P} \frac{n_H^2}{n_S} \right) / \left(1 + \left(\frac{n_H}{n_L} \right)^{2P} \frac{n_H}{n_S} \right) \right]^2$$

> Bandpass filters transmit a range of λ and block the rest

> Short pass edge filters transmit all shorter λ

> Long pass edge filters transmit all larger λ

> Dichroic filters reflect specific λ and transmit others

} at 0°

at 45°

Temperature and Space Environment Impact

> A thin film has a different n for a different T , also thus changing the reflectance

↳ They also have thermal expansion

> In space, there is:

- ① Radiation
- ② Temperature extremes
- ③ Atomic oxygen
- ④ Vacuum
- ⑤ Contamination

↳ These all lead to degradation

LECTURE 11: RADIO WAVES AND SUB-MM INSTRUMENTS

> Radar, sonar, lidar all use wave reflections to detect objects
↳ Radio ↳ Sound ↳ Light

↳ Radar is an active instrument

↳ A single antenna is used for transmission and reception

↳ A single pulse is transmitted, reflected, and the propagation time measured

↳ Reflectivity and scattering affect the reflection

$$\text{Range} = \frac{c t_R}{2}$$

> For a uniformly radiating antenna transmitting over a sphere

$$\text{Power density} = \frac{P_t}{4\pi R^2}$$

> For a directive antenna:

$$\text{Emitted} = \frac{P_t G_t}{4\pi R^2} ; G = 4\pi \frac{A_{\text{eff}}}{\lambda^2} ; A_{\text{eff}} = A K$$

$$\text{Received} = \frac{P_t G_t}{4\pi R^2} A_r = \frac{P_t G_t}{4\pi R^2} \frac{G_r \lambda^2}{4\pi} = \frac{P_t G_t G_r \lambda^2}{(4\pi R)^2}$$

> For the monostatic case, the transmitter is the receiver

↳ The target only intercepts and reflects a portion of the emission corresponding to its cross-sectional area

$$\text{Reflected} = \frac{P_t G_t}{4\pi R^2} \sigma$$

↳ Also, it is not considered a flat mirror

$$\text{Reflected P.D.} = \frac{P_t G_t}{(4\pi R^2)^2} \sigma$$

$$\text{Received} = \frac{P_t G_t^2 \lambda^2 \sigma}{(4\pi)^3 R^4}$$

> For the bistatic case, the transmitter is not the receiver

$$P_r = \frac{P_t G_t G_r \lambda^2 \sigma}{(4\pi)^3 R_t^2 R_r^2}$$

> Pulsed radar sends high f pulses with width τ

$$\text{Range resolution } \Delta R = \frac{c\tau}{2} = \frac{c}{2\text{BW}}$$

↳ is the ability to distinguish 2 or more sources in the same bearing but at different ranges

> A continuous wave can be frequency modulated f sweep

↳ Detector receives an echo

$$4 S = \frac{c \Delta t}{2} = \frac{c \Delta f \frac{dt}{df}}{2} = c \Delta f / 2 \frac{df}{dt}$$

> Radio wave detectors can measure both amplitude and phase of the EM fields (VIS-IR only)

> We can observe binary asteroids using delay-Doppler techniques

$$4 B = \frac{4\pi D}{\lambda P} \cos \gamma$$

> With several layers, there will be an echo delay between the signals

$$4 P_{ss} = P_t \left(\frac{\sqrt{G}\lambda}{8\pi(H+z)} \right)^2 T_s^2 R_{ss} e^{-2\pi f \tan \delta t}$$

> We can see different reflections from layer composition

> LiDAR can be used for surface topology

LECTURE 12: LASER BASED INSTRUMENTS (1)

- > Why:
 - ① Dependency on others
 - ② Need for connection

↳ Currently, wireless is done mainly through RF as it is robust and mature

↳ RF suffers from **divergence**

$$\theta_{div} = \frac{2.44}{D} \lambda$$

↳ This causes power loss, interference, ...

↳ As laser has a lower λ , θ_{div} is lower

Challenges

- ① Pointing (low θ_{div})
- ② Clouds occlusion and fog
- ③ Atmospheric attenuation
- ④ Atmospheric turbulence
- ⑤ Sun blinding

$$\theta_{div} = \frac{\lambda}{\pi w_0}$$

$$D_{spot} = 2 \cdot \theta_{div} \cdot L$$

- > Other issues:
 - ① Background radiation
 - ② Wavefront errors
 - ③ Laser safety

System Choices and Applications

> The OSI model consists of several layers for proper communication

↳ The **physical layer** consists of:

- ① Transmitter

↳ Data source, encoder, laser, modulator, booster EDFA

- ② Medium

↳ 2 optical systems, free space

- ③ Receiver

↳ Pre-amp EDFA, demodulator, decoder

> We use the O, S, C, L, and E bands for communications

↳ Most work is done at 1550 nm (C-band) as it is the optimum (minimal loss)

- > Operational phases:
- ① Acquisition
 - ② Tracking
 - ③ Communication

Performance

- > Key performance goals:
- ① High throughput
 - ② Quasi error free
 - ③ High availability
 - ④ Low latency

- u With:
- ① Low cost
 - ② Low bandwidth
 - ③ safe
 - ④ small
 - ⑤ Low complexity

> A link budget shows how much power can be lost in the link

$$P_R = P_T \cdot G_i \cdot L_i$$

$$P_{Rx} = \underbrace{P_{Tx}}_{\text{Transmitter}} + \underbrace{G_{Tx} - L_{Tx}}_{\text{Medium}} - \underbrace{L_{Rx}}_{\text{Receiver}} \quad [\text{dB}]$$

> Free space loss $L_{FS} = \left(\frac{4\pi r}{\lambda}\right)^2$

$$G_{Tx} = \frac{S}{\Theta_{div}^2} = 2 \left(\frac{2\pi w_0}{\lambda}\right)^2$$

$$G_{Rx} = \left(\frac{\pi D_R}{\lambda}\right)^2$$

> The channel capacity is the maximum achievable data rate

$$C = B \log_2 \left(1 + \frac{S}{N}\right)$$

Gaussian Beams

> Gaussian beams are propagation invariant

$$I(r, z) = \underbrace{I_0}_{\text{source}} \underbrace{\left(\frac{w_0}{w(z)}\right)^2}_{\text{axial}} \underbrace{e^{-\left(r^2/w(z)^2\right)}}_{\text{radial}}$$

u The width propagates over a distance

$$w(z) = w_0 \cdot \sqrt{1 + (z/Z_R)^2} \quad ; \quad Z_R = \pi w_0^2 n / \lambda \quad \rightarrow \text{Rayleigh range}$$

$$\Theta_{div} = \frac{\lambda}{\pi n w_0}$$

Pointing Errors

- ① Static
- ② Dynamic pointing jitter

u Results in loss of power and scintillation

$$\textcircled{1} > T_{p,e} = e^{-2\Theta_{p,e}^2 / \Theta_{d,u}^2} ; \Theta_{p,e} = \frac{r}{L}$$

> There is a trade-off between pointing error and divergence

$$\textcircled{2} > T_{p,a} = \frac{\Theta_{d,u}^2}{\Theta_{d,u}^2 + 4\kappa_{ij}^2}$$

$$> T_{p,s} = P_0 \frac{4\sigma_{ij}^2}{\Theta_{d,u}^2}$$

LECTURE 13: LASER BASED INSTRUMENTS (2)

Pointing Systems Architecture

> A passive system consists of a telescope, mirrors, beam splitter, transmitter, and receiver

↳ Various pointing systems can be added:

- ① Body pointing
- ② Coarse pointing assembly
- ③ Fine steering method
- ④ Point ahead mirror

② ↳ Requirements:

- ① Large range
- ② Medium-high resolution
- ③ 2 axis steering
- ④ Low transmission losses

↳ Types:

- ① Periscope

↳ 2 mirrors
↳ Rotation perpendicular to optical axis

② Prism based

↳ light propagates through prisms
↳ No cable wraps required

③ Gimbal

↳ Rotate the entire terminal
↳ No movement in optical system

③ ↳ Requirements:

- ① Small range
- ② High bandwidth
- ③ Low residual error
- ④ 2 axis tilt

↳ For precise control of motion

↳ Consists of:

- ① Mirror
- ② Sensors
- ③ Actuators
- ④ Hinge
- ⑤ RTC

④ ↳ There is a loss due to movement of the satellites in the link

↳ A PAM points the mirror at the angle between tx and rx beam

> The tracking detector either uses an image or a quad cell

> A control loop is present for the tracking controller

↳ Typically PID

Turbulence

> Turbulence causes a fluctuation of n in the light path

↳ Driven by T differences $\rightarrow$ wind shear and buoyancy

↳ Causes image distortion and blur

> Regions:

- ① Energy injection
- ② Energy transfer
- ③ Dissipation

> Atmospheric turbulence causes:

- ① Beam wander
- ② Beam spread
- ③ Scintillation
- ④ AOA fluctuations
- ⑤ Spot widening

①

$$\sigma_{BW}^2 = 0.54 \left(\frac{\lambda}{D} \right)^2 \left(\frac{D}{r_0} \right)^{5/3}$$

↳ Similar to jitter

②③

↳ Wider beam with equal energy

$$S_{BS} = \left(1 + \left(\frac{D_0}{r_0} \right)^{5/3} \right)^{-6/5}$$

$$L_{SC} = (3.3 - 5 + 7 \sqrt{-\ln P_{out}}) \sigma_I^{4/5}$$

④

$$\sigma_{\alpha}^2 = 0.18 \left(\frac{D}{r_0} \right)^{5/3} \left(\frac{\lambda}{D} \right)^2$$

ADD-ON FROM EXERCISES

> **Bit Error Rate** is the ratio of wrong over total bits

↳ Function of normalized bit energy E_b and variance of noise σ^2

$$↳ E_b = \left(\frac{1_i - 1_o}{2} \right)^2$$

$$↳ \text{BER} = \frac{1}{2} \text{erfc} \left(\sqrt{E_b / 2\sigma^2} \right)$$

$$↳ \text{SNR} = E_b / \sigma^2$$

LECTURE 14: HIGH ENERGY IMAGERS

> X-rays and γ -rays are very high energy, and thus have high penetration power

↳ Classification:

- ① Soft X
- ② Classical X
- ③ Hard X
- ④ γ

> X-rays are emitted by:

- ① Thermal (BB, bremsstrahlung)
- ② Nonthermal (collisions, scattering, synchrotron)

- ①
- ↳ Black body emission emits in X-ray for very high T
 - ↳ Thermal bremsstrahlung occurs in high T environments, produced by fast moving free e^- being deflected by a proton
- ②
- ↳ Collisional bremsstrahlung has an e^- colliding with an atom, emitting a bound e^-
 - ↳ Characteristic X-rays happen when an inner e^- is ejected and replaced by a higher energy e^-
 - ↳ Inverse Compton is when a low energy photon collides with a relativistic e^- , emitting energy at the expense of the e^-
 - ↳ Synchrotron emission happens when a relativistic particle spirals in an electric field

> Energy spectra:

- ① Power law
- ② Black body
- ③ Thermal bremsstrahlung

> γ -rays are created in:

- ① Radioactive decay
- ② Nuclear fission
- ③ High energy collisions, secondary

> Pretty much all stars emit X-rays

Detection

> Challenges:

- ① Penetrating power
- ② Background noise
- ③ General space mission problems

> A **Soller collimator** uses angular filtering, limiting divergence

> If a ray glances the surface, it will reflect, and not penetrate, happening for the **grazing incidence**

↳ A Walter telescope uses this to focus the rays at one point

> Diffraction gratings can also be used

> Detectors:

- ① Proportional counters
- ② Microchannel plates
- ③ Semiconductors
- ④ CCD
- ⑤ Micro-calorimeters

-0.5
-1
-1
-0.5
1

> The resolving power depends on the type used — 1

LECTURE 15: INSTRUMENTS FOR CHARGED PARTICLES

> We have sub-nuclear particles and nuclear particles

> We can measure:

① Charge	} for charged particles
② Momentum	
③ Track	
④ Type	
⑤ Flux	
⑥ Dose	
⑦ Dose rate	

> In space, we have radiation due to:

- ① Trapped particles
- ② Solar energetic particles
- ③ Cosmic rays

> To detect particles in space, they need to reach the monitor, and interact with it

> A detector has 3 parts:

- ① Absorber
- ② Observable phenomenon from the interaction
- ③ Measuring method

> When interacting with the e^- , the particle loses energy and the atoms become excited or ionized

> When interacting with the nucleus, the particle is deflected causing scattering

> Cherenkov radiation happens when $v_p > c$ in the medium

> At a boundary crossing, an X-ray photon may be created transition radiation

> The energy loss $-(\frac{dE}{dx})_{coll}$ is described by the Bethe-Bloch formula

↳ This has 4 zones:

- ① Fast decrease
- ② Minimum energy loss
- ③ Slow relativistic increase
- ④ Constant loss per unit length

> Energy loss depends on material and particle mass

> Detector types:

- ① Ionization
- ② Scintillation
- ③ Solid state